# In-person session 6

**February 15, 2024**

PMAP 8521: Program evaluation
Andrew Young School of Policy Studies

# Plan for today

DAGs

Logic models, DAGs, and measurement

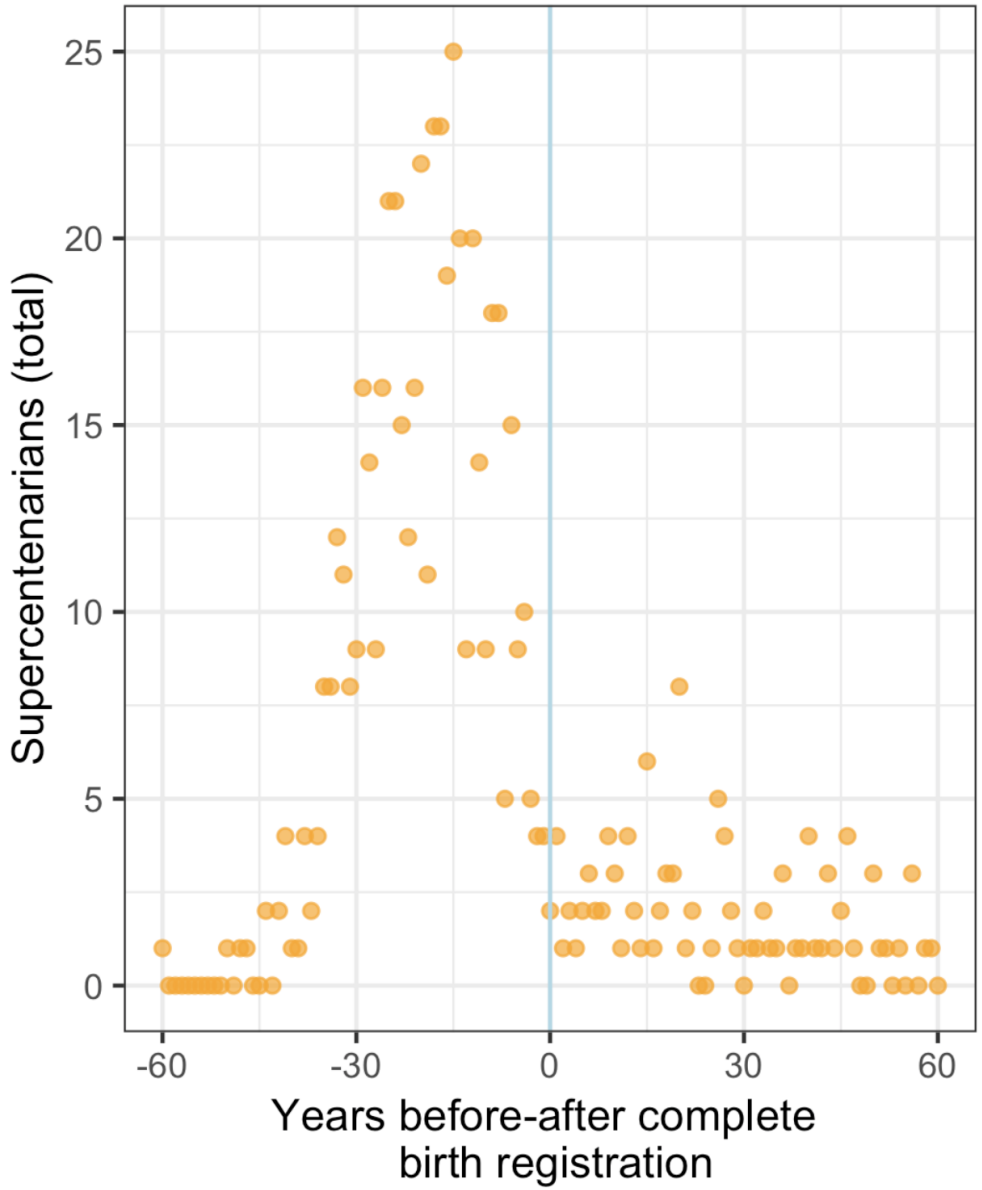
Potential outcomes vs. do() notation

do-calculus, adjustment, and CATEs

# Exam 1 details

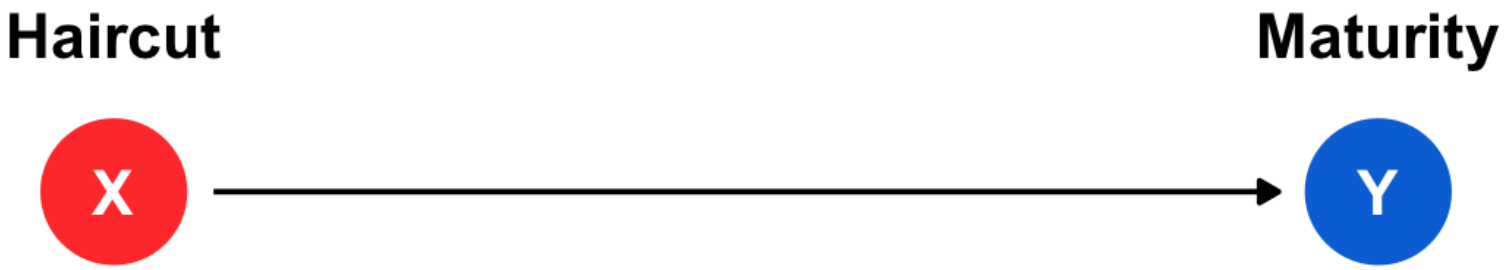
# DAGs

# Causal thinking is necessary—even for descriptive work!


Supercentenarians (total)
25
20
15
10
5
0
-60
-30
0
30
60
Years before-after complete
birth registration

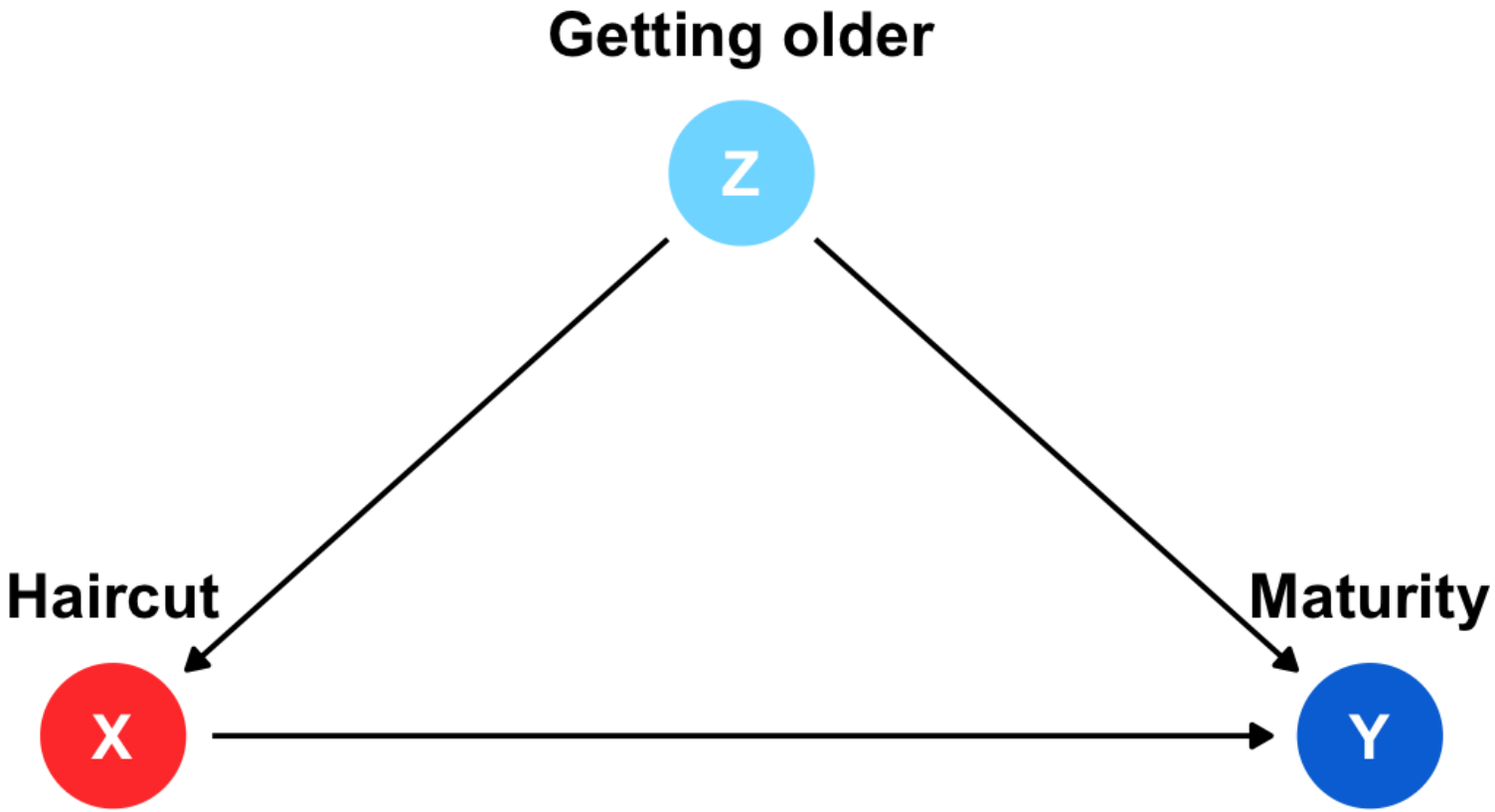
# "Every time I get a haircut, I become more mature!"

# "Every time I get a haircut, I become more mature!"

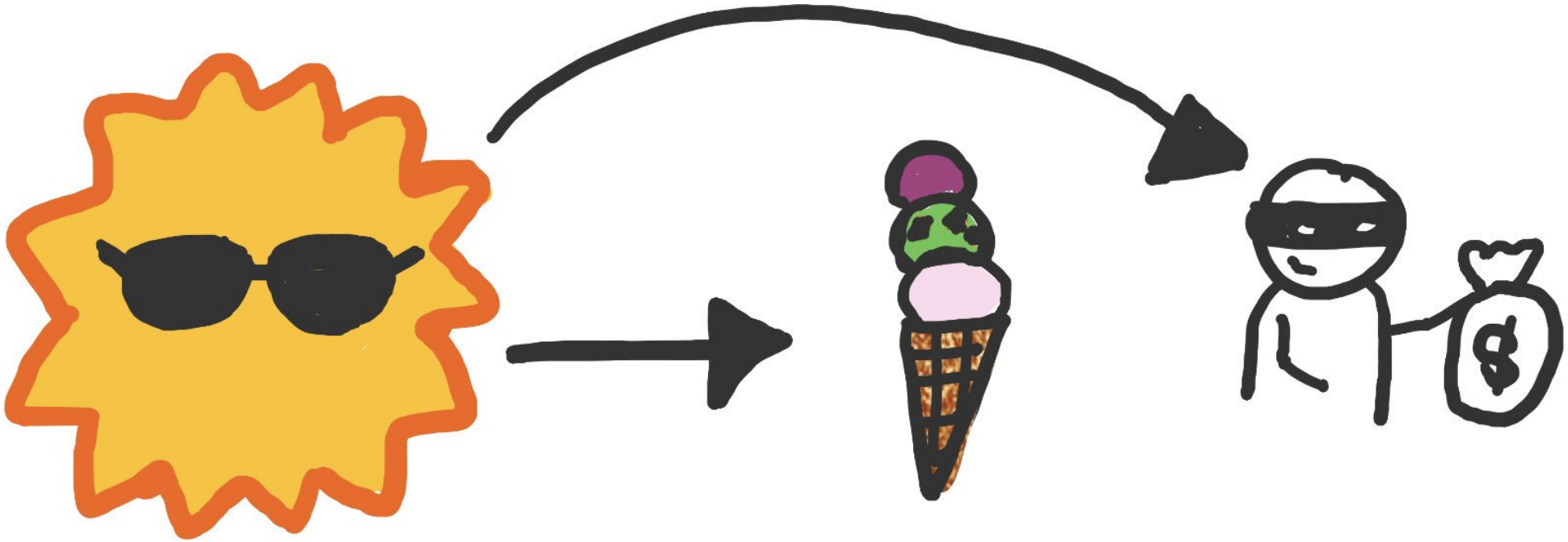



$$E[\text{Maturity} \mid \text{do}(\text{Get haircut})]$$

# Getting older opens a backdoor path



# Ice cream causes crime



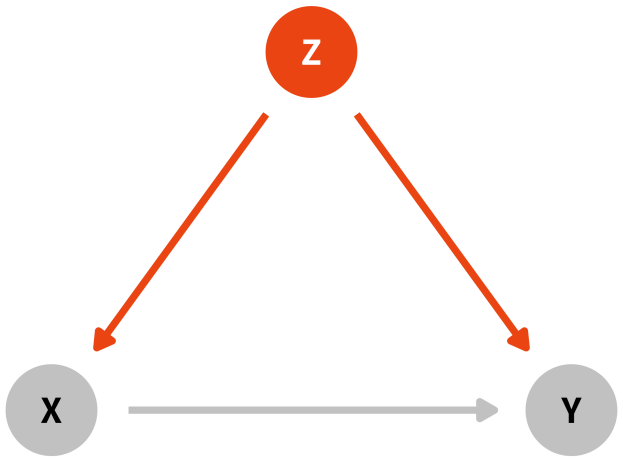
**Summer weather opens a backdoor path**

**But what does that mean, "opening a backdoor path"?**

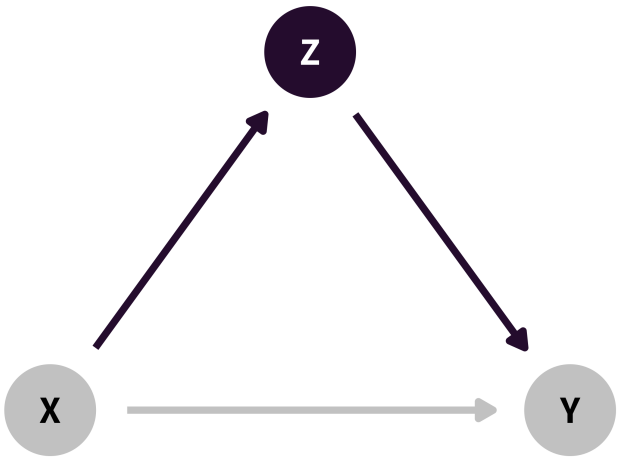
**How does statistical association get passed through paths?**

# How do I know which of these is which?

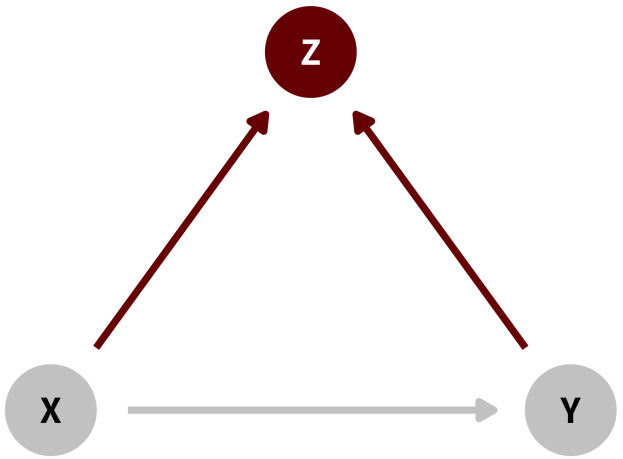
**Confounder**
(Fork)



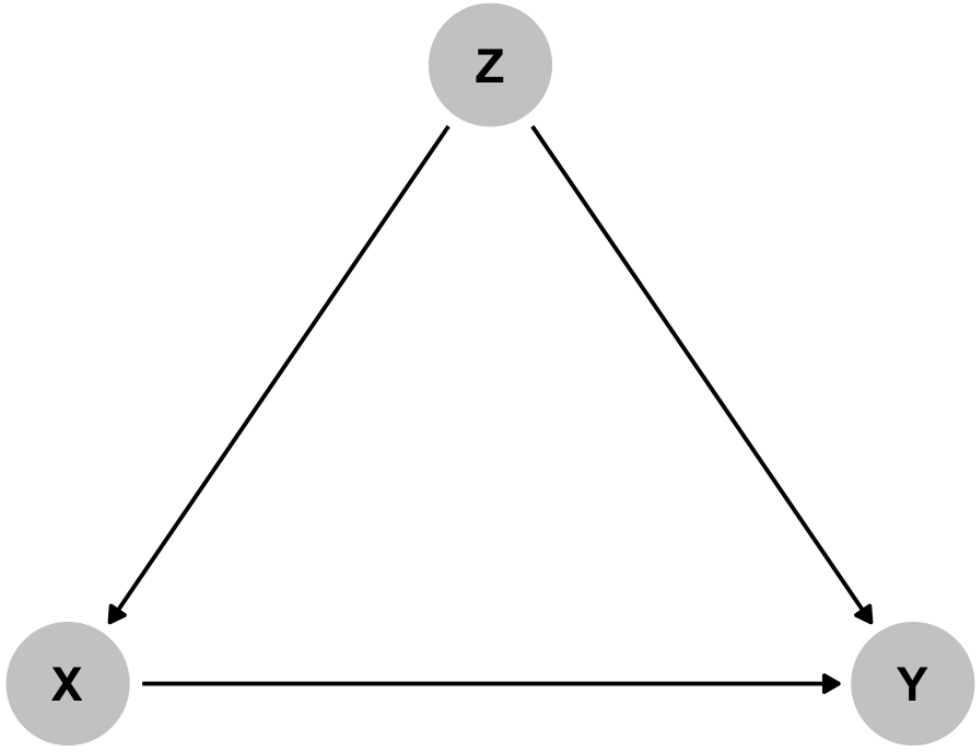

**Mediator**
(Chain)



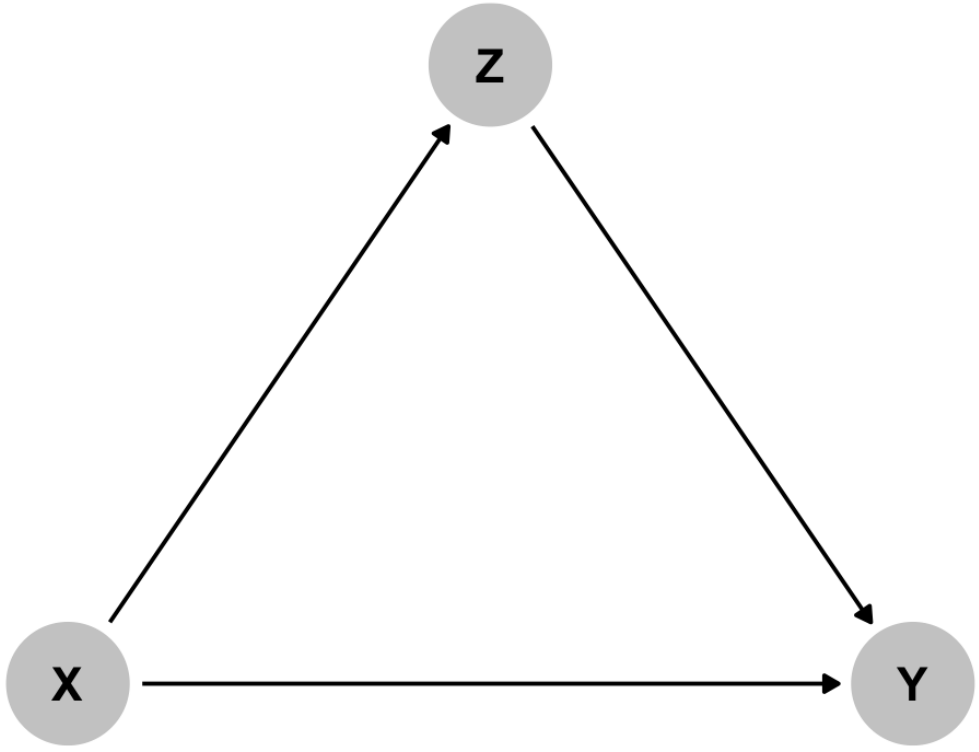

**Collider**
(Inverted fork)



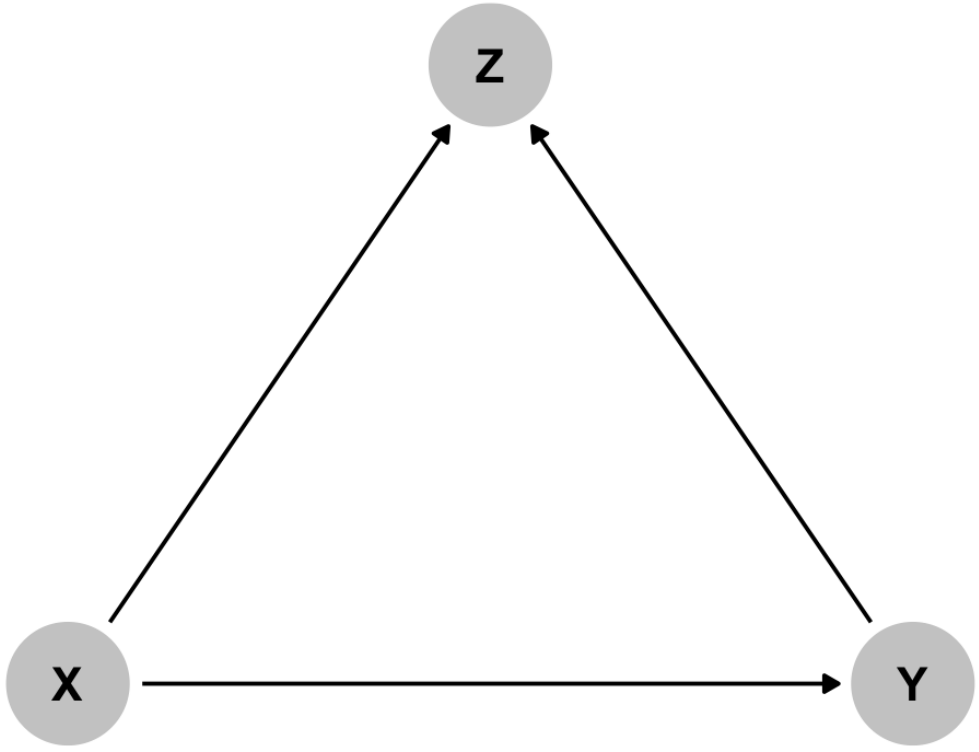

LUTRON

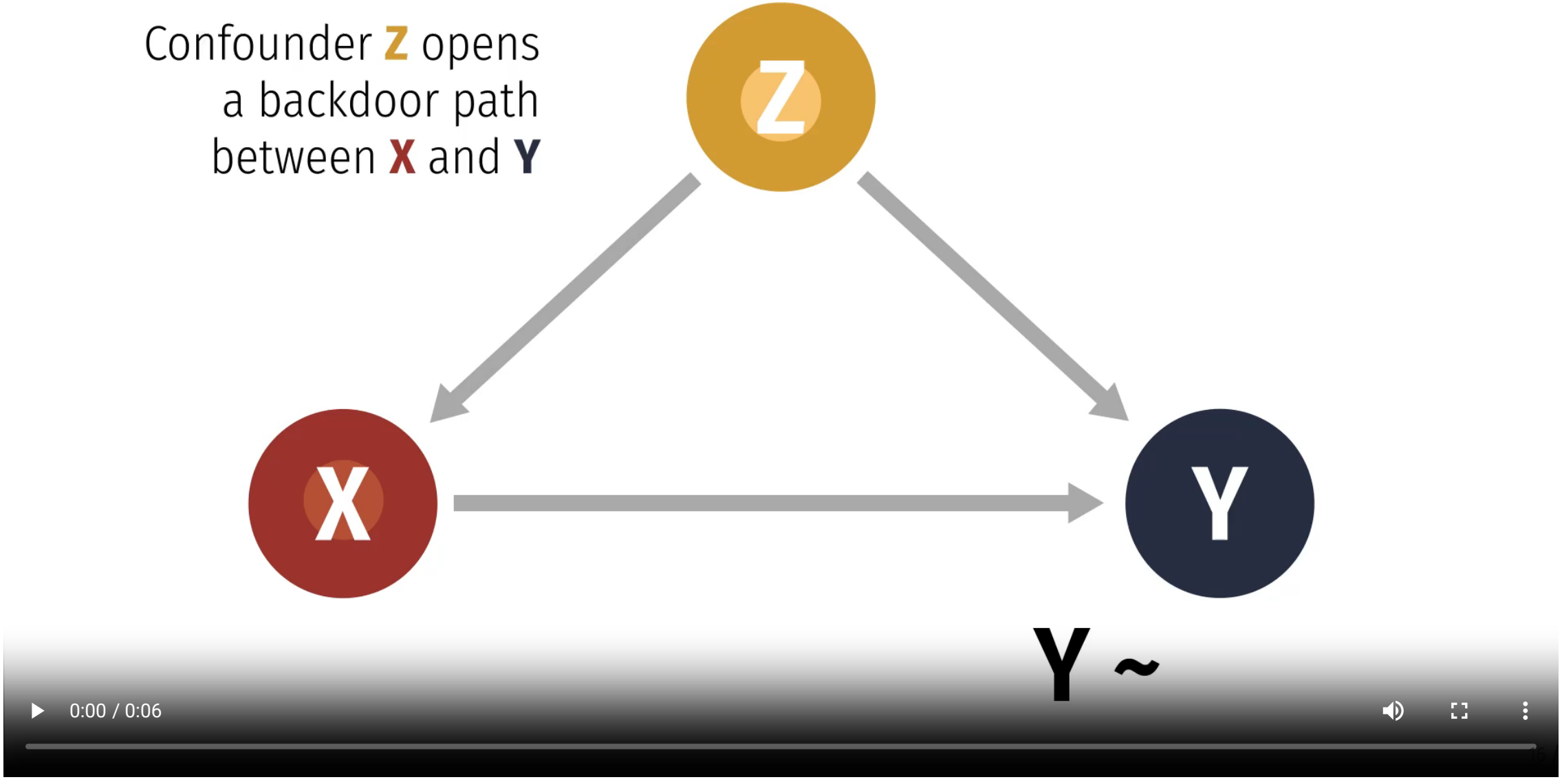

Z
X
Y

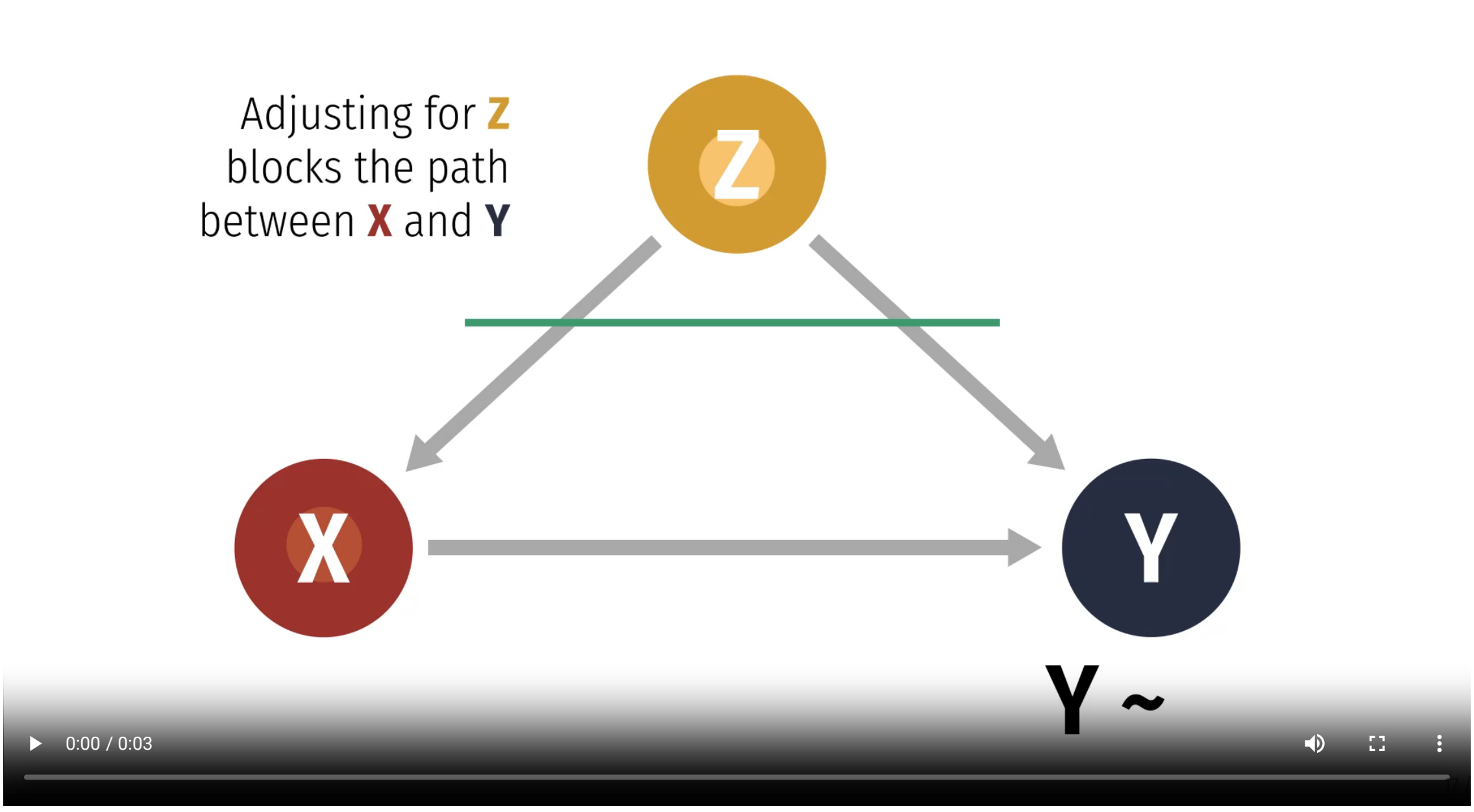

LUTRON

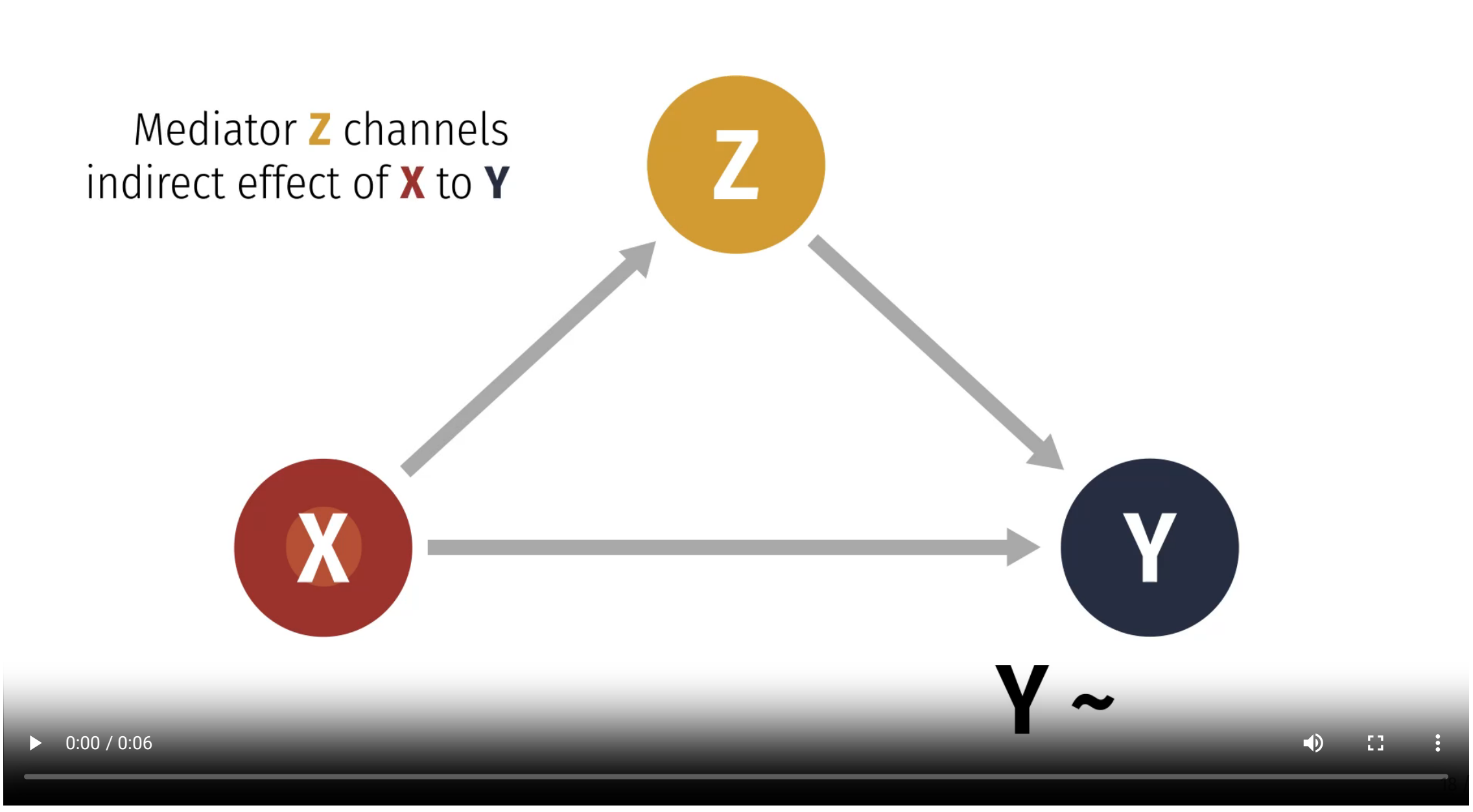

Z
X
Y


LUTRON


Z
X
Y


Confounder Z opens
a backdoor path
between X and Y
Z
X
Y
Y ~
0:00 / 0:06


Adjusting for Z
blocks the path
between X and Y
Z
X
Y
Y ~
0:00 / 0:03


Mediator Z channels
indirect effect of X to Y
Z
X
Y
Y ~
0:00 / 0:06

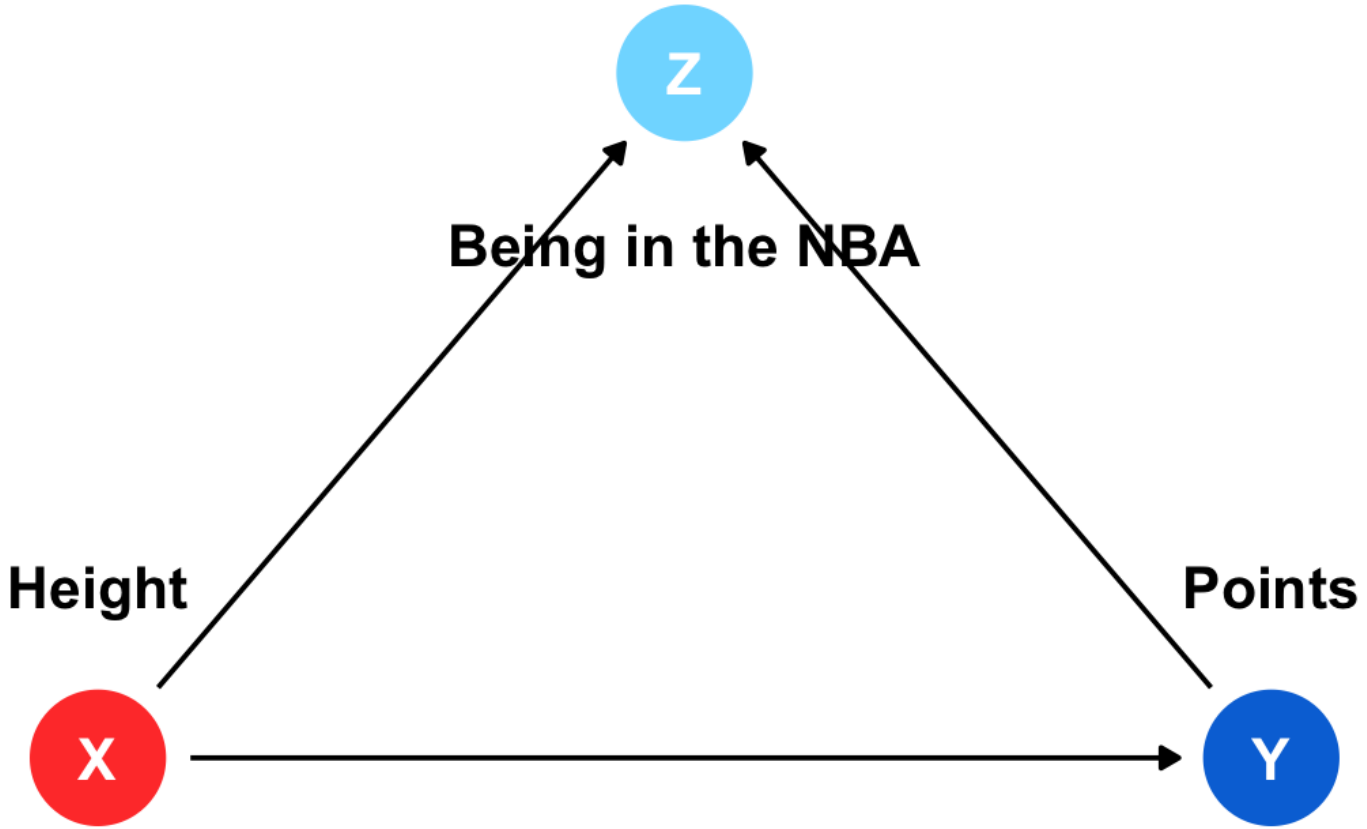
# d-separation

Except for the one arrow between X and Y,
no statistical association can flow between X and Y

This is **identification**—
all alternative stories are ruled out
and the relationship is isolated

# How exactly do colliders mess up your results?

## It looks like you can still get the effect of X on Y

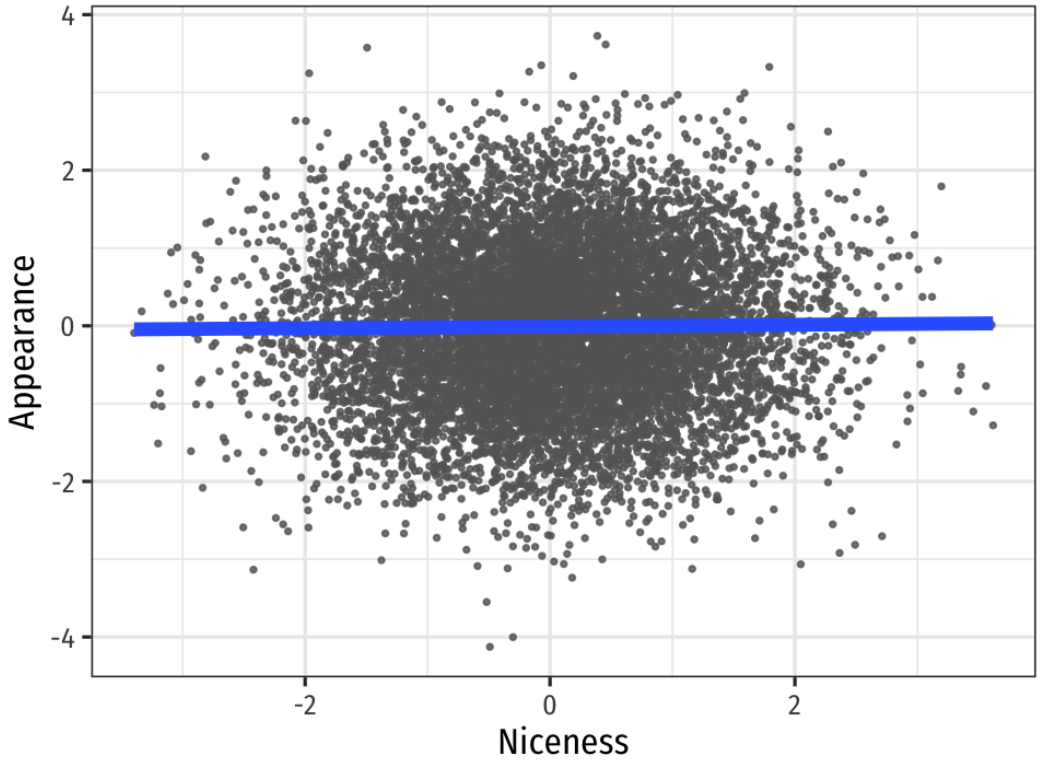

Z
Being in the NBA
Height
Points
X
Y

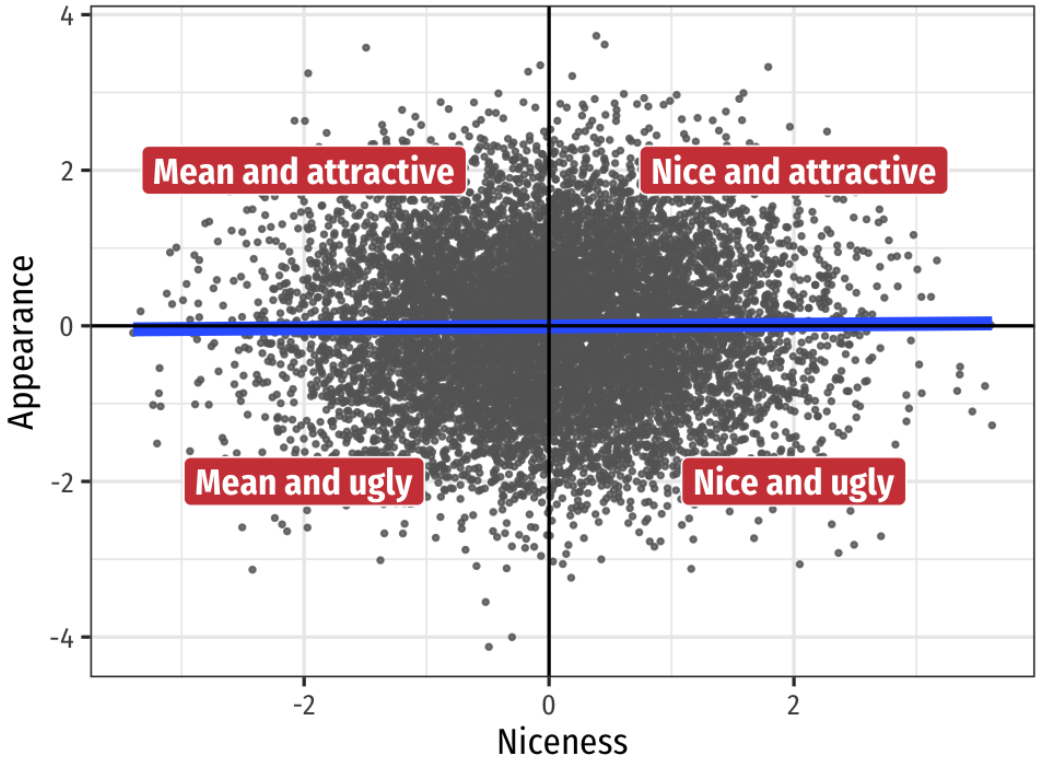
**Sept. 10, 2021, 3:58 p.m. ET**
By Davey Alba

# Facebook sent flawed data to misinformation researchers.

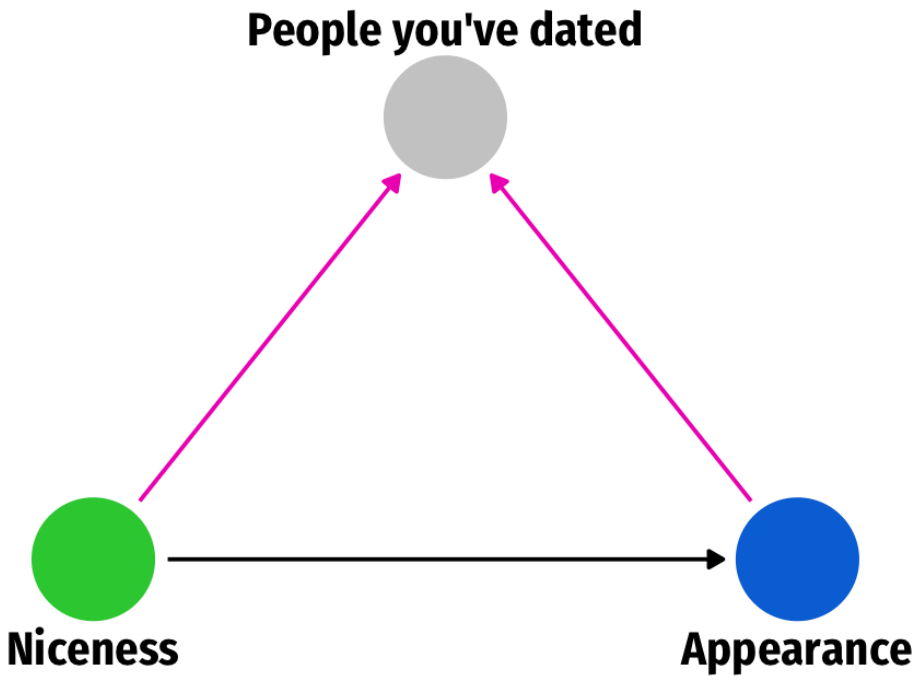
Mark Zuckerberg, chief executive of Facebook, testifying in Washington in 2018. Tom Brenner/The New York Times

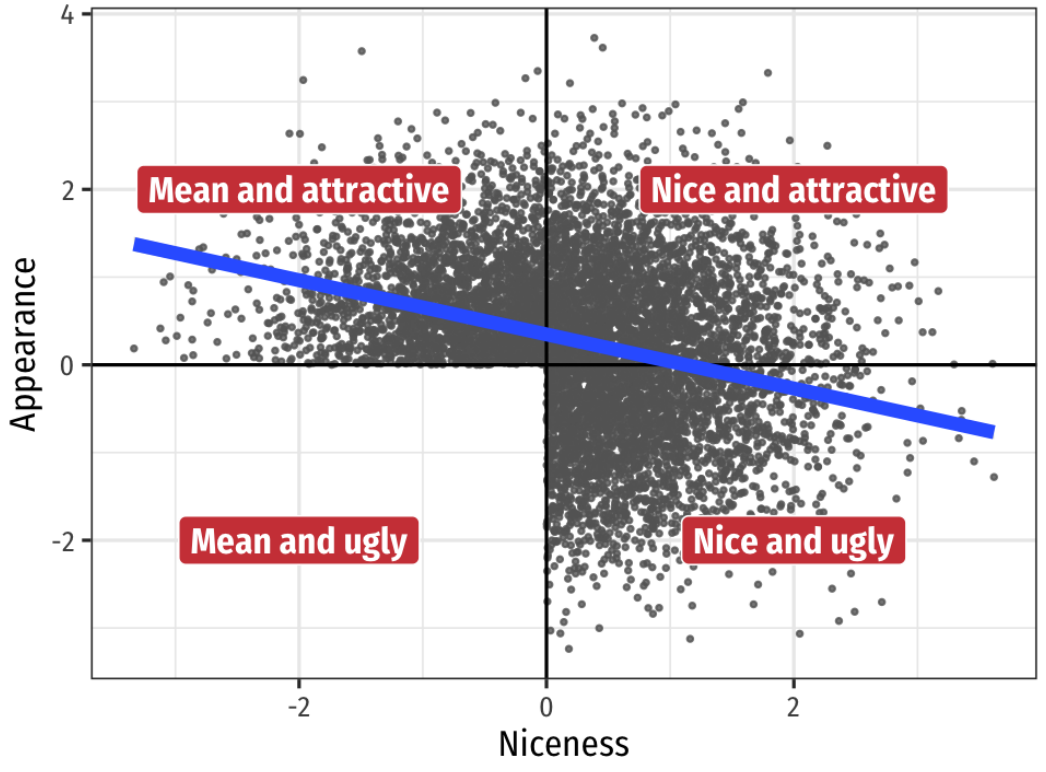
# Does niceness improve appearance?

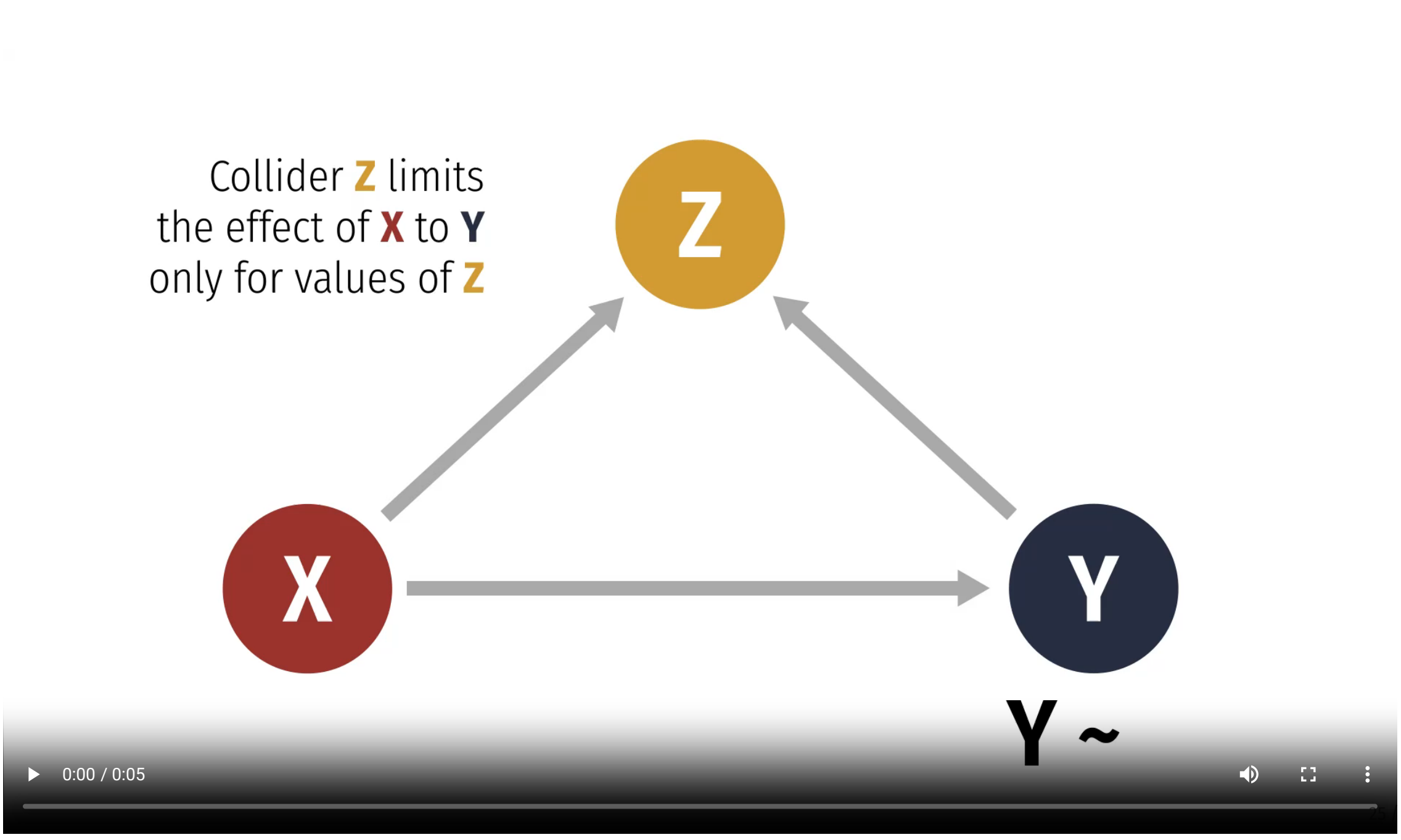


# Collider distorts the true effect!

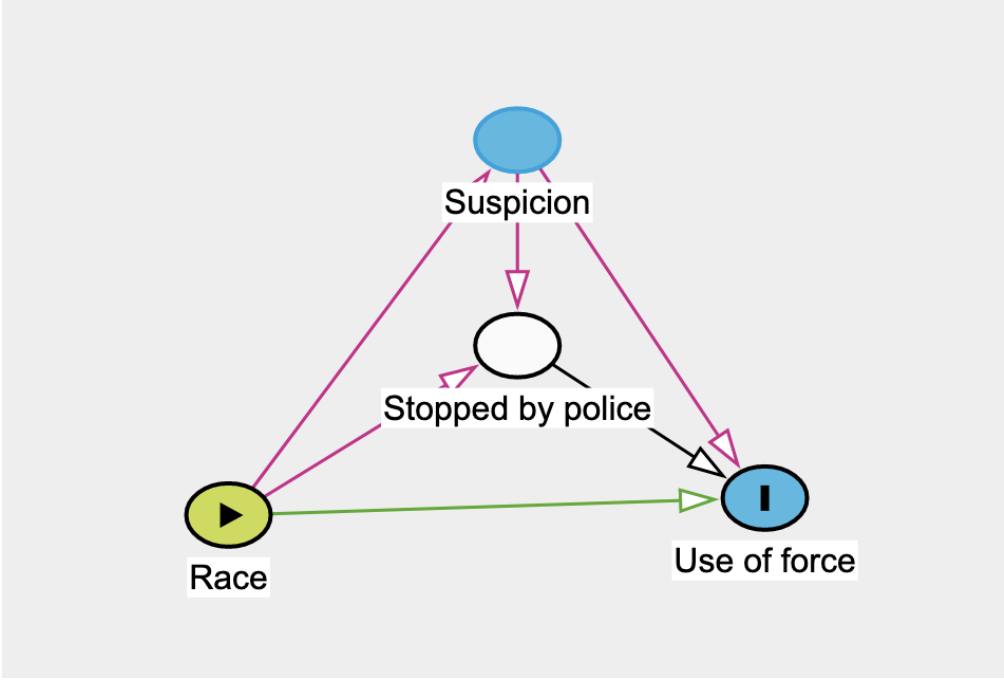



Collider Z limits
the effect of X to Y
only for values of Z
Z
X
Y
Y ~
0:00 / 0:05

# Effect of race on police use of force using administrative data

# Effect of race on police use of force using administrative data




*American Political Science Review*, Page 1 of 19
doi:10.1017/S0003055420000039


## Administrative Records Mask Racially Biased Policing

DEAN KNOX *Princeton University*
WILL LOWE *Hertie School of Governance*
JONATHAN MUMMOLO *Princeton University*

*Researchers often lack the necessary data to credibly estimate racial discrimination in policing. In particular, police administrative records lack information on civilians police observe but do not investigate. In this article, we show that if police racially discriminate when choosing whom to investigate, analyses using administrative records to estimate racial discrimination in police behavior are statistically biased, and many quantities of interest are unidentified—even among investigated individuals—absent strong and untestable assumptions. Using principal stratification in a causal mediation framework, we derive the exact form of the statistical bias that results from traditional estimation. We develop a bias-correction procedure and nonparametric sharp bounds for race effects, replicate published findings, and show the traditional estimator can severely underestimate levels of racially biased policing or mask discrimination entirely. We conclude by outlining a general and feasible design for future studies that is robust to this inferential snare.*

Concern over racial bias in policing, and the public availability of large administrative data sets documenting police–civilian interactions, have prompted a raft of studies attempting to quantify the effect of civilian race on law enforcement behavior. These studies consider a range of outcomes including ticketing, stop duration, searches, and the use of force (e.g., Antonovics and Knight 2009; Fryer 2019; Ridgeway 2006; Nix et al. 2017). Most research in this area attempts to adjust for omitted variables that may correlate with suspect race and the outcome of interest. In contrast, this study addresses a more fundamental problem that remains even if the vexing issue of omitted variable bias is solved: the inevitable statistical bias that results from studying racial discrimination using records that are themselves the product of racial discrimination (Angrist and Pischke 2008; Elwert and Winship 2014; Rosenbaum 1984). We show that when there is any biased absent additional data and/or strong and untestable assumptions.

This study makes several contributions. We clarify the causal estimands of interest in the study of racially discriminatory policing—quantities that many studies appear to be targeting, but are rarely made explicit—and show that the conventional approach fails to recover any known causal quantity in reasonable settings. Next, we highlight implicit and highly implausible assumptions in prior work and derive the statistical bias when they are violated. We proceed to develop informative nonparametric sharp bounds for the range of possible race effects, apply these in a reanalysis and extension of a prominent article on police use of force (Fryer 2019), and present bias-corrected results that suggest this and similar studies drastically underestimate the level of racial bias in police–civilian interactions. Finally, we outline strategies for future data collection and re-

# Smoking → Cardiac arrest example

**How do you know if the DAG is right??**

**How can you be sure you include everything in a DAG?**

**How do you know when to stop?**

**Is there a rule of thumb for the number of nodes?**

**Why can we combine nodes in a DAG if they don't represent the same concept?**

**Why include unmeasurable things in a DAG?**

**Why do DAGs have to be acyclic?**

**What if there really is reverse causation?**

# How do we actually adjust for these things?

# Logic models, DAGs, and measurement

# What's the difference between logic models and DAGs?

Can't I just remake my logic model in Dagitty and be done?

# DAGs vs. Logic models

## DAGs are a *statistical* tool

Describe a data-generating process and isolate/identify relationships

## Logic models are a *managerial* tool

Oversee the inner workings of a program and its theory

# Berkeley Will Fully Close Its Streets to Create Giant Outdoor Dining Rooms

3

Berkeley is moving fast to expand outdoor dining

by Eve Batey | May 14, 2020, 1:02pm PDT

SHARE




# How cities can add accessible green space in a post-coronavirus world

June 11, 2020 3.40pm EDT

Cities can prepare for climate change emergencies by adding green spaces to help manage stormwater, heat stress and air quality. (Shutterstock)



The COVID-19 pandemic has forced governments to weigh the benefits of keeping green spaces open against the public health concerns that come from their use. During the pandemic, playgrounds have been taped off, parks locked and access to outdoor spaces for recreation cut off.

Green spaces have positive effects on mental health, physical fitness, social cohesion and spiritual wellness. Although researchers say the coronavirus spreads more easily indoors than outdoors, they also believe the concentrated use of green spaces will increase the transmission of COVID-19.

Authors

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# Potential outcomes vs. do() notation

# Expectations

$$\mathbf{E}(\cdot), \mathbf{E}(\cdot), \mathbb{E}(\cdot) \quad \text{vs.} \quad \mathbf{P}(\cdot)$$

**Basically a fancy way of saying "average"**

# Potential outcomes and CATEs example

# Why can't we just subtract the averages between treated and untreated groups?

# When you're making groups for CATE, how do you decide what groups to put people in?

Slides from lecture

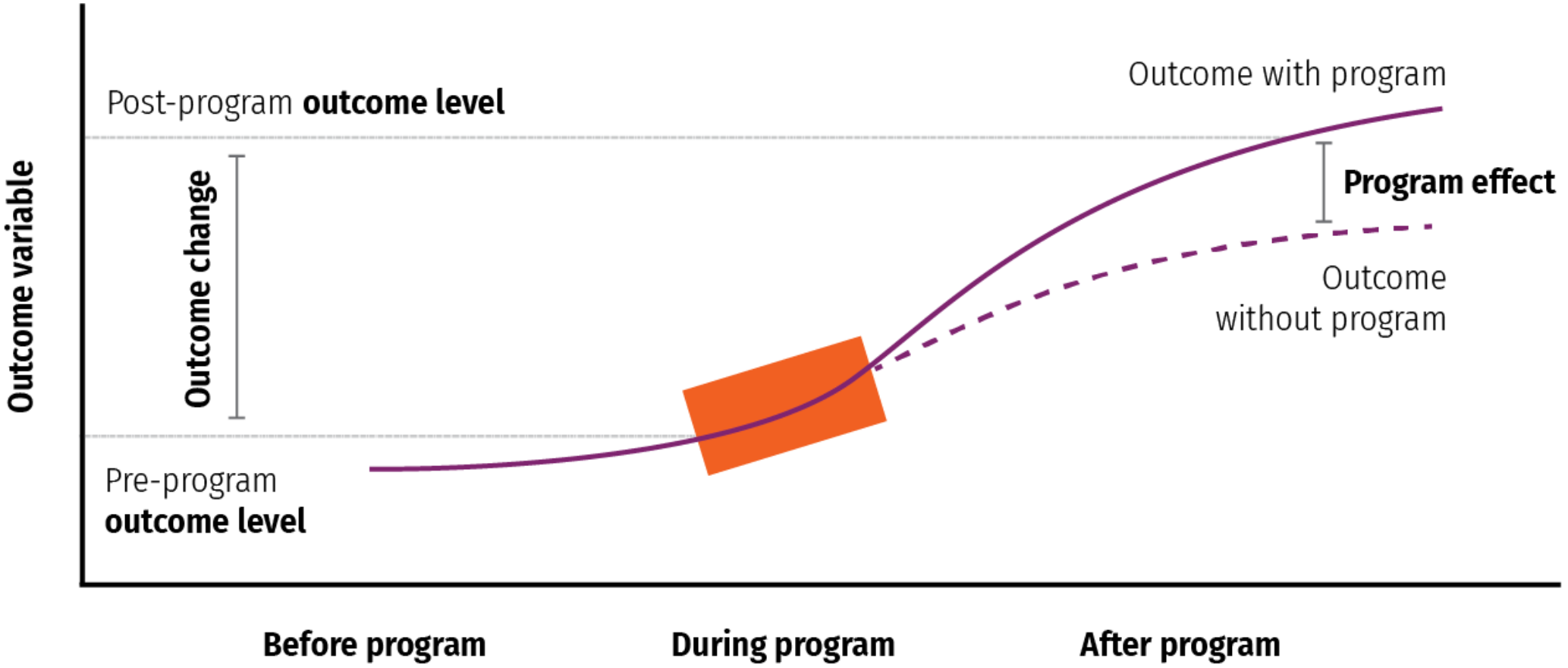
# Unconfoundedness assumption

**How can we assume/pretend that treatment was randomly assigned within each age?**

**It seems unlikely. Wouldn't there be other factors within the older/younger group that make a person more/less likely to engage in treatment (e.g., health status)?**

Slides from lecture

# Outcomes and programs



# Causal effects with potential outcomes

**Potential outcomes notation:**

$$\delta = \frac{1}{n} \sum_{i=1}^{n} Y_i(1) - Y_i(0)$$

or alternatively with $\mathbf{E}$

$$\delta = \mathbf{E}[Y_i(1) - Y_i(0)]$$

# Causal effects with do()

**Pearl notation:**

$$\delta = \mathbf{E}[Y_i \mid \text{do}(X = 1) - Y_i \mid \text{do}(X = 0)]$$

or more simply

$$\delta = \mathbf{E}[Y_i \mid \text{do}(X)]$$

$$\mathbf{E}[Y_i \mid \mathrm{do}(X)]$$

$$=$$

$$\mathbf{E}[Y_i(1) - Y_i(0)]$$

**We can't see this**

$$\mathbf{E}[Y_i \mid \text{do}(X)] \quad \text{or} \quad \mathbf{E}[Y_i(1) - Y_i(0)]$$

**So we find the average causal effect (ACE)**

$$\hat{\delta} = \mathbf{E}[Y_i \mid X = 1] - \mathbf{E}[Y_i \mid X = 0]$$

The average population-level change in $y$ when *directly intervening* (or doing) $x$

The average population-level change in $y$ when accounting for *observed* $x$

$$\mathbf{E}(y \mid \text{do}(x)) \neq \mathbf{E}(y \mid x)$$

Causation

Correlation

# do-calculus and adjustment

# DAGs and identification

DAGs are a statistical tool, but they don't tell you what statistical method to use

DAGs help you with the **identification strategy**

**Thomas Massie**
@RepThomasMassie

Over 70% of Americans who died with COVID, died on Medicare, and some people want #MedicareForAll ?

11:00 AM · Feb 9, 2022 · Twitter for iPhone

# Easist identification

## Identification through research design

RCTs

**When treatment is randomized, delete all arrows going into it**

## No need for any do-calculus!

# Most other identification

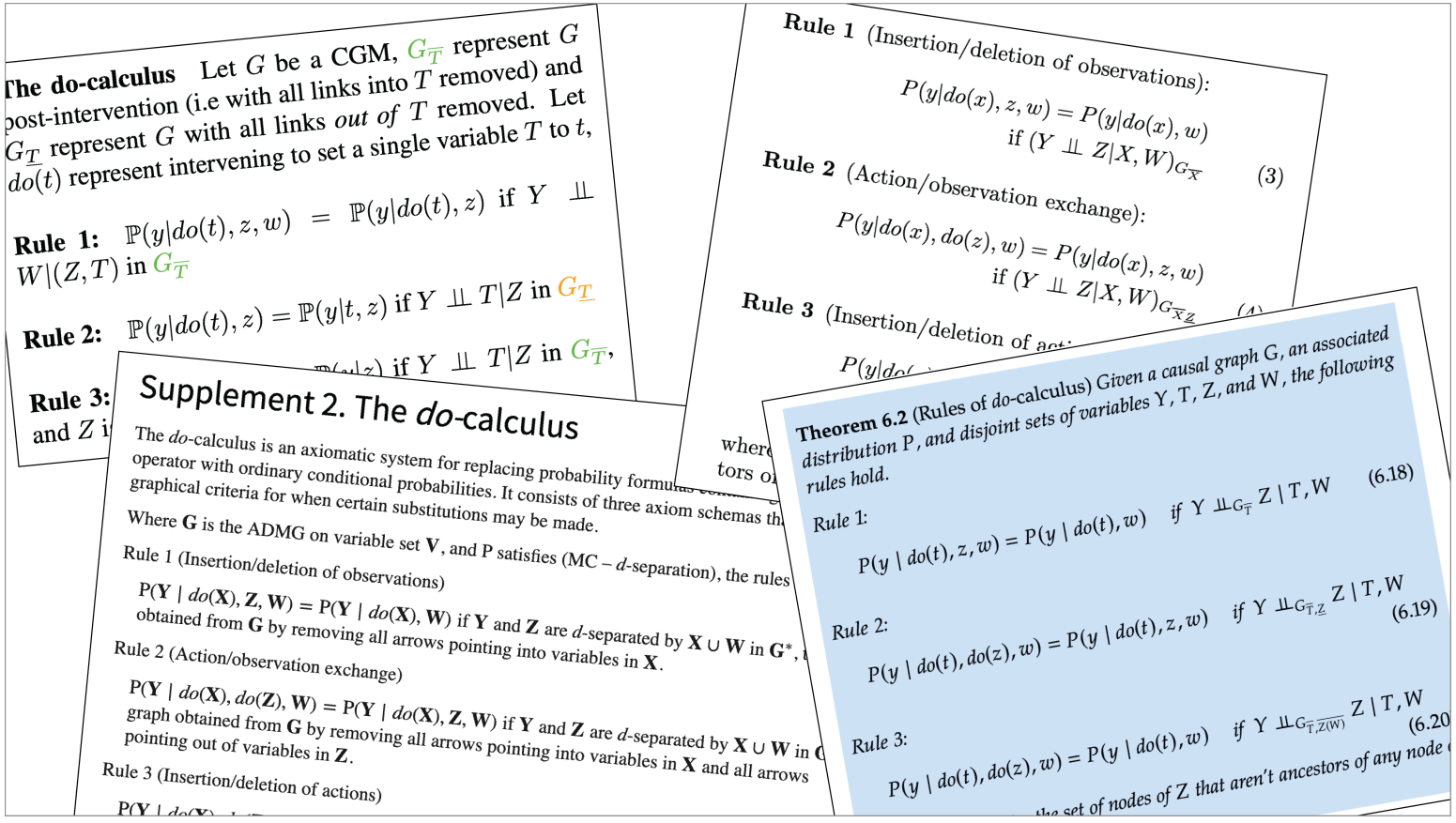
## Identification through do-calculus

### Rules for graph surgery

**Backdoor adjustment and frontdoor adjustment are special common patterns of do-calculus**

# Where can we learn more about *do*-calculus?

Here!



**Rule 1**: Decide if we can ignore an observation

$$P(y \mid z, \mathrm{do}(x), w) = P(y \mid \mathrm{do}(x), w) \qquad \text{if } (Y \perp Z \mid W, X)_{G_{\overline{X}}}$$

**Rule 2**: Decide if we can treat an intervention as an observation

$$P(y \mid \mathrm{do}(z), \mathrm{do}(x), w) = P(y \mid z, \mathrm{do}(x), w) \qquad \text{if } (Y \perp Z \mid W, X)_{G_{\overline{X},\underline{Z}}}$$

**Rule 3**: Decide if we can ignore an intervention

$$P(y \mid \mathrm{do}(z), \mathrm{do}(x), w) = P(y \mid \mathrm{do}(x), w) \qquad \text{if } (Y \perp Z \mid W, X)_{G_{\overline{X},\overline{Z(W)}}}$$

$$
\begin{aligned}
&\text{[Marginalization across } z + \text{ chain rule for conditional probabilities]} \\
P(y \mid \text{do}(x)) &= \sum_z P(y \mid \text{do}(x), z) \times P(z \mid \text{do}(x)) \\
&\text{[Use Rule 2 to treat do}(x) \text{ as } x\text{]} \\
&= \sum_z P(y \mid x, z) \times P(z \mid \text{do}(x)) \\
&\text{[Use Rule 3 to nuke do}(x)\text{]} \\
&= \sum_z P(y \mid x, z) \times P(z \mid \text{nothing!}) \\
&\text{[Final backdoor adjustment formula!]} \\
&= \sum_z P(y \mid x, z) \times P(z)
\end{aligned}
$$

# Adjusting for backdoor confounding

Causal effect of $x$ on $y$

Conditional mean of $y$, given $x$ and $z$...

... weighted by $z$

$$\mathbf{E}(y \mid \text{do}(x)) = \sum_{z} \mathbf{E}(y \mid x, z) \times \mathbf{P}(z)$$

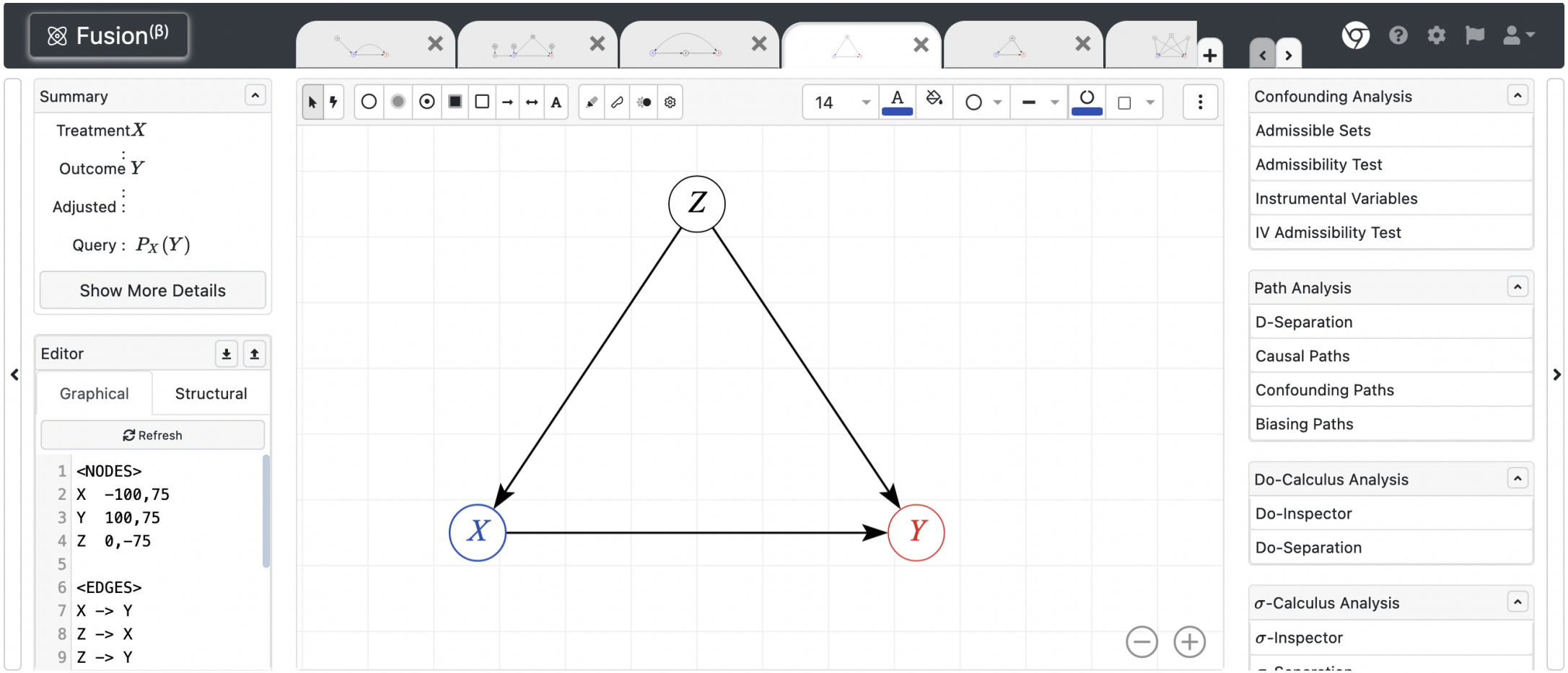
Sum across all values of $z$

# Adjusting for frontdoor confounding

# More complex DAGs without obvious backdoor or frontdoor solutions

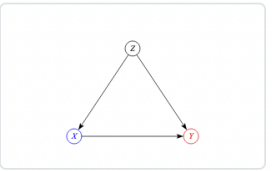
## Chug through the rules of do-calculus to see if the relationship is identifiable

Causal Fusion


Fusion(β)
Summary
Treatment $X$
Outcome $Y$
Adjusted :
Query : $P_X(Y)$
Show More Details
Editor
Graphical
Structural
Refresh
<NODES>
X -100,75
Y 100,75
Z 0,-75
<EDGES>
X -> Y
Z -> X
Z -> Y
14
Z
X
Y
Confounding Analysis
Admissible Sets
Admissibility Test
Instrumental Variables
IV Admissibility Test
Path Analysis
D-Separation
Causal Paths
Confounding Paths
Biasing Paths
Do-Calculus Analysis
Do-Inspector
Do-Separation
σ-Calculus Analysis
σ-Inspector

Compute | The causal effect of X on Y conditional on  with do : | (Query: $P_X(Y)$ ) | Non-Parametric | Clear

1 $$P_X(Y) = \sum_Z P(Y|X,Z)\,P(Z)$$



Load | Estimation | Derivation | Remove

**Simplified** Obtained by Back-Door adjustment with an admissible set $\{Z\}$

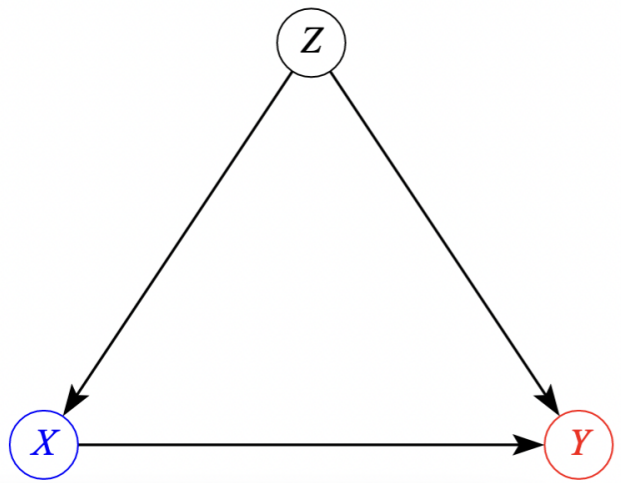
Do-Calculus

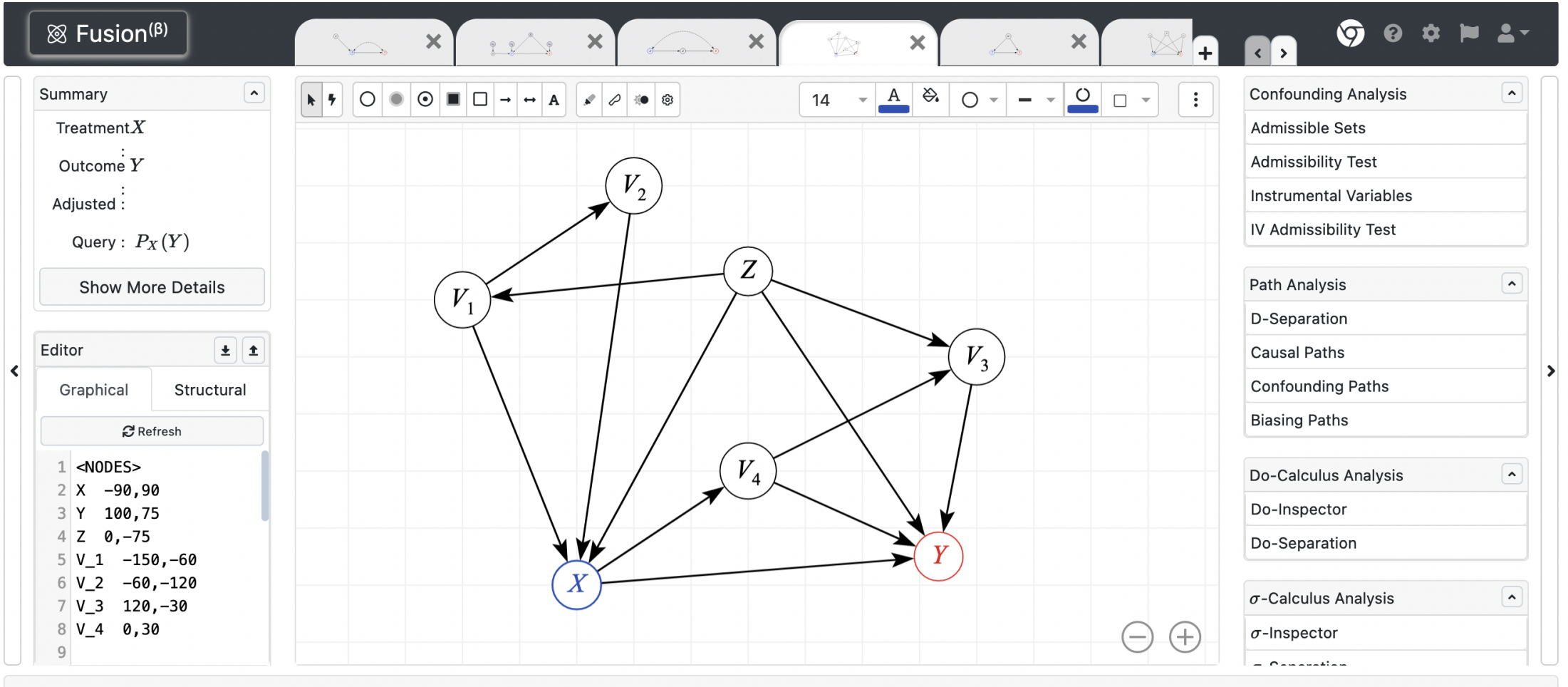
- $P_X(Y)$ (1)
  - $\sum_Z P_X(Y|Z)\,P_X(Z)$ Summing over: $Z$ (2)
    - $\sum_Z P(Y|X,Z)\,P_X(Z)$ Rule 2: $(X \perp Y|Z)_{G_{\underline{X}}}$ (3)
      - $\sum_Z P(Y|X,Z)\,P(Z)$ Rule 3: $(X \perp Z)_{G_{\overline{X}}}$ (4)

Finally we get: $\sum_Z P(Y|X,Z)\,P(Z)$

Subgraph:

☐ Show non-active nodes/edges




Fusion(β)
Summary
Treatment $X$
Outcome $Y$
Adjusted :
Query : $P_X(Y)$
Show More Details
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Refresh
<NODES>
X -90,90
Y 100,75
Z 0,-75
V_1 -150,-60
V_2 -60,-120
V_3 120,-30
V_4 0,30
14
$V_1$
$V_2$
$Z$
$V_3$
$V_4$
$X$
$Y$
Confounding Analysis
Admissible Sets
Admissibility Test
Instrumental Variables
IV Admissibility Test
Path Analysis
D-Separation
Causal Paths
Confounding Paths
Biasing Paths
Do-Calculus Analysis
Do-Inspector
Do-Separation
σ-Calculus Analysis
σ-Inspector

Compute | The causal effect of X on Y conditional on  with do : | (Query: $P_X(Y)$ ) | Non-Parametric | Clear

1 $P_X(Y)$ is not identifiable from $P(V_1, V_2, V_3, V_4, X, Y, Z)$ and $P_X(V_1, V_2, V_3,$

Load | Remove

**When things are identified, there are still arrows leading into Y.**
**What do we do with those?**
**How do you explain those relationships?**

**Outcomes have multiple causes.**
**How do you justify that your proposed cause is the most causal factor?**

# Does every research question need an identification strategy?

**No!**

**Correlation alone is okay!**
**Can lead to more focused causal questions later!**

Forbes

BREAKING | Jan 14, 2022, 12:34pm EST | 145,393 views

# Moderna Starts Human Trials Of mRNA Vaccine For Virus That Likely Causes Multiple Sclerosis

**Robert Hart** Forbes Staff
Business
*I cover breaking news.*

Follow

Listen to article 3 minutes

**TOPLINE** Moderna recently launched early stage clinical trials for an mRNA vaccine against the Epstein-Barr virus (EBV), a common pathogen that infects almost everyone at some point in their lives, is the primary cause of mononucleosis and, according to a study published in the journal *Science* Thursday, likely causes multiple sclerosis (MS), offering hope the devastating neurological condition might be prevented.